

## Solving Equations with Variables on Both Sides Classwork

**Aim:** How can we determine the solution of an equation with variables on both sides?

**Warm Up:** Solve the following equations

(a)  $3(x - 2) - 3 = 4 + \frac{1}{2}(12x + 14)$

$$3x - 6 - 3 = 4 + 6x + 7$$

$$3x - 9 = 11 + 6x$$

$$\begin{array}{r} 3x - 9 = 11 + 6x \\ +9 \quad +9 \\ \hline 3x = 20 + 6x \\ -6x \quad -6x \\ \hline -3x = 20 \\ \frac{-3x}{-3} = \frac{20}{-3} \end{array} \quad x = -\frac{20}{3}$$

(b)  $5 - 2(x - 10) = 50$

$$5 - 2x + 20 = 50$$

$$-2x + 25 = 50$$

$$\begin{array}{r} -2x + 25 = 50 \\ -25 \quad -25 \\ \hline -2x = 25 \\ \frac{-2x}{-2} = \frac{25}{-2} \end{array} \quad x = -\frac{25}{2}$$

**Guided Practice:**

Exercise 1- Solve the following equations

**I Do:**

$$6x - 3(x - 1) = 4(2x + 1)$$

$$6x - 3x + 3 = 8x + 4$$

$$3x + 3 = 8x + 4$$

$$\begin{array}{r} 3 = 5x + 4 \\ -4 \quad -4 \\ \hline -1 = 5x \end{array}$$

$$\frac{-1}{5} = \frac{5x}{5}$$

$$x = -\frac{1}{5}$$

**You Try:**

$$3(x - 1) - (4x + 2) = 9(x + 3)$$

$$3x - 3 - 4x - 2 = 9x + 27$$

$$-x - 5 = 9x + 27$$

$$\begin{array}{r} -5 = 10x + 27 \\ -27 \quad -27 \\ \hline -32 = 10x \end{array}$$

$$\frac{-32}{10} = \frac{10x}{10}$$

$$x = -\frac{16}{5}$$

Exercise 2- Solve the following equations (Proportions)

**I Do:**

$$\frac{x - 6}{9} = \frac{x + 9}{4}$$

$$4(x - 6) = 9(x + 9)$$

$$4x - 24 = 9x + 81$$

$$\begin{array}{r} -24 = 5x + 81 \\ -81 \quad -81 \\ \hline -105 = 5x \end{array}$$

$$\frac{-105}{5} = \frac{5x}{5}$$

$$x = -21$$

**You Try:**

$$\frac{7}{2x - 8} = \frac{3}{x - 6}$$

$$7(x - 6) = 3(2x - 8)$$

$$7x - 42 = 6x - 24$$

$$\begin{array}{r} x - 42 = -24 \\ +42 \quad +42 \\ \hline x = 18 \end{array}$$

$$x = 18$$

Exercise 3- Solve the following equations (with Multiplying Polynomials)

I Do:

$$x(x-9) = (x+3)(x-8)$$

$$x^2 - 9x = x^2 - 8x + 3x - 24$$

$$\begin{array}{r} x^2 - 9x = x^2 - 8x + 3x - 24 \\ -x^2 \quad \quad -x^2 \\ \hline \end{array}$$

$$\begin{array}{r} -9x = -5x - 24 \\ +5x \quad +5x \\ \hline \end{array}$$

$$\begin{array}{r} -4x = -24 \\ -4 \quad \quad -4 \\ \hline x = 6 \end{array}$$

You Try:

$$(2x-5)(3x-2) = 3x(2x-6)$$

$$6x^2 - 4x - 15x + 10 = 6x^2 - 18x$$

$$\begin{array}{r} 6x^2 - 19x + 10 = 6x^2 - 18x \\ -6x^2 \quad \quad -6x^2 \\ \hline \end{array}$$

$$\begin{array}{r} -19x + 10 = -18x \\ +19x \quad \quad +19x \\ \hline \end{array}$$

$$10 = x$$

Problem Set: Solve the following for questions then complete "solving equations hangman"

$$-4\left(\frac{1}{2}x - 0.4\right) = 1.3 - 0.6(0.3 - 0.2x)$$

$$-2x + .16 = 1.3 - .18 - .12x$$

$$\begin{array}{r} -2x + .16 = 1.12 - .12x \\ +.2x \quad \quad +.2x \\ \hline \end{array}$$

$$\begin{array}{r} .16 = 1.12 + .08x \\ -1.12 \quad -1.12 \\ \hline \end{array}$$

$$-.96 = .08x$$

$$x = -12$$

$$\frac{1}{4}\left(5x + \frac{16}{3}\right) - \frac{2}{3}\left(\frac{3}{4}x + \frac{1}{2}\right) = -5$$

$$\frac{5}{4}x + \frac{4}{3} - \frac{1}{2}x - \frac{1}{3} = -5$$

$$\begin{array}{r} \frac{3}{4}x + \frac{8}{3} = -5 \\ -\frac{8}{3} \quad -\frac{8}{3} \\ \hline \end{array}$$

$$\frac{3}{4}x = -6$$

$$x = -8$$

$$(x+3)^2 = x(x+2) - 3$$

$$(x+3)(x+3) = x^2 + 2x - 3$$

$$\begin{array}{r} x^2 + 6x + 9 = x^2 + 2x - 3 \\ -x^2 \quad \quad -x^2 \\ \hline \end{array}$$

$$\begin{array}{r} 6x + 9 = 2x - 3 \\ -9 \quad \quad -9 \\ \hline \end{array}$$

$$\begin{array}{r} 6x = 2x - 12 \\ -2x \quad -2x \\ \hline \end{array}$$

$$\begin{array}{r} 4x = -12 \\ 4 \quad \quad 4 \\ \hline \end{array}$$

$$x = -3$$

$$\frac{x-4}{2} = \frac{x+2}{3}$$

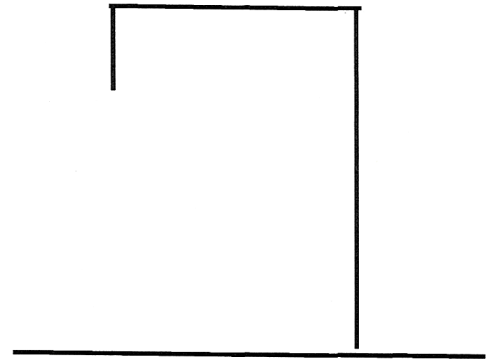
$$2(x+2) = 3(x-4)$$

$$\begin{array}{r} 2x + 4 = 3x - 12 \\ -2x \quad \quad -2x \\ \hline \end{array}$$

$$\begin{array}{r} 4 = x - 12 \\ +12 \quad \quad +12 \\ \hline \end{array}$$

$$16 = x$$

# Solving Linear Equations Hangman Activity



P
O
L
Y
N
O
M
I
A
L

4      8.25      -18.825      6      60      8.25       $-11\frac{1}{3}$        $-\frac{9}{7}$       8.3      -18.825

<b>A</b> $4(x - 7) = 0.3(x + 2) + 2.11$	<b>I</b> $3x - 2(x + 4) = 8x + 1$	<b>O</b> $\frac{7}{3}\left(x + \frac{9}{28}\right) = 20$
<b>B</b> $-4(x - 3) = 5(2x - 6)$	<b>J</b> $\frac{x}{2.8} - 4.9 = -7.11$	<b>P</b> $\frac{x - 2}{3} + \frac{1}{6} = \frac{5}{6}$
<b>C</b> $5(x + 2) - 1.5x = 6$	<b>K</b> $\frac{7}{4}(b - 1) = \frac{7}{8}$	<b>R</b> $-7x - 4x = 8 - 2x - 8x$
<b>D</b> $3(x - 2) + 5 = 2(5x - 4)$	<b>L</b> $\frac{5}{6}\left(\frac{3}{8} - x\right) = 16$	<b>S</b> $-8(1 + 4x) + 7x = -25 - 8x$
<b>E</b> $\frac{3}{4}x + 2 = \frac{5}{4}x - 6$	<b>M</b> $\frac{2}{3}\left(\frac{1}{4}x - 2\right) = \frac{1}{5}\left(\frac{4}{3}x - 1\right)$	<b>T</b> $\frac{19}{4} - 3.5x = -.25x + \frac{3}{2}$
<b>H</b> $\frac{9}{4} = -\frac{3}{2}x + \frac{19}{4}$	<b>N</b> $\frac{3}{4}x + 8 = x - 7$	<b>Y</b> $\frac{1}{7} + \frac{2x}{3} = \frac{15x - 3}{21}$



### Hangman Workspace

Goal - Solve the hidden message. Choose a letter and solve that equation in the space below. Check the solution to the following equation in your calculator. Add a body part to the board if your answer doesn't exist on one of those lines. Then, pick another letter and continue the steps.

<p><u>A</u></p> $4(x-7) = .3(x+2) + 2.11$ $4x - 28 = .3x + .6 + 2.11$ $4x - 28 = .3x + 2.71$ $\begin{array}{r} 4x - 28 = .3x + 2.71 \\ - .3x \quad - .3x \\ \hline 3.7x = 30.71 \\ \frac{3.7x}{3.7} = \frac{30.71}{3.7} \end{array}$ <p><math>x = 8.3</math></p>	<p><u>N</u></p> $\frac{3}{4}x + 8 = x - 7$ $\begin{array}{r} \frac{3}{4}x + 8 = x - 7 \\ - \frac{3}{4}x \quad - 8 \\ \hline \frac{3}{4}x = x - 15 \\ - \frac{3}{4}x \quad - x \\ \hline -\frac{1}{4}x = -15 \\ \frac{-\frac{1}{4}x}{-\frac{1}{4}} = \frac{-15}{-\frac{1}{4}} \\ x = 60 \end{array}$
<p><u>P</u></p> $\frac{x-2}{3} + \frac{11}{6} = \frac{5}{6}$ $\begin{array}{r} \frac{x-2}{3} + \frac{11}{6} = \frac{5}{6} \\ - \frac{11}{6} \quad - \frac{11}{6} \\ \hline \frac{x-2}{3} = \frac{5}{6} - \frac{11}{6} \\ \frac{x-2}{3} = \frac{-6}{6} \\ \frac{x-2}{3} = -1 \\ x-2 = -3 \\ x = -1 \end{array}$ <p><math>6x - 12 = 12</math></p> $\begin{array}{r} 6x - 12 = 12 \\ + 12 \quad + 12 \\ \hline 6x = 24 \\ \frac{6x}{6} = \frac{24}{6} \\ x = 4 \end{array}$	<p><u>M</u></p> $\frac{2}{3} \left( \frac{1}{4}x - 2 \right) = \frac{1}{5} \left( \frac{4}{3}x - 1 \right)$ $\frac{1}{6}x - \frac{4}{3} = \frac{4}{15}x - \frac{1}{5}$ $\begin{array}{r} \frac{1}{6}x - \frac{4}{3} = \frac{4}{15}x - \frac{1}{5} \\ - \frac{1}{6}x \quad - \frac{4}{3} \\ \hline -\frac{4}{3} = \frac{1}{10}x - \frac{1}{5} \\ + \frac{1}{5} \quad + \frac{1}{5} \\ \hline -\frac{4}{3} + \frac{1}{5} = \frac{1}{10}x \\ -\frac{20}{15} + \frac{3}{15} = \frac{1}{10}x \\ -\frac{17}{15} = \frac{1}{10}x \\ x = -11.333 \end{array}$
<p><u>O</u></p> $\frac{7}{3} \left( x + \frac{9}{28} \right) = 20$ $\frac{7}{3}x + \frac{3}{4} = 20$ $\begin{array}{r} \frac{7}{3}x + \frac{3}{4} = 20 \\ - \frac{3}{4} \quad - \frac{3}{4} \\ \hline \frac{7}{3}x = \frac{77}{4} \\ \frac{7}{3}x = \frac{77}{4} \end{array}$ <p><math>x = 8.25</math></p> <p><math>x = \frac{33}{4}</math></p>	
<p><u>L</u></p> $\frac{5}{6} \left( \frac{3}{8} - x \right) = 16$ $\frac{5}{16} - \frac{5}{6}x = 16$ $\begin{array}{r} \frac{5}{16} - \frac{5}{6}x = 16 \\ - \frac{5}{16} \quad - \frac{5}{16} \\ \hline -\frac{5}{6}x = \frac{251}{16} \\ x = \frac{-753}{40} \\ x = -18.825 \end{array}$	<p><u>I</u></p> $3x - 2(x+4) = 8x + 1$ $3x - 2x - 8 = 8x + 1$ $x - 8 = 8x + 1$ $\begin{array}{r} x - 8 = 8x + 1 \\ -x \quad -x \\ \hline -8 = 7x + 1 \\ -1 \quad -1 \\ \hline -9 = 7x \\ x = -\frac{9}{7} \end{array}$
<p><u>Y</u></p> <del><math display="block">2 \left( \frac{3 \cdot 1}{7} + \frac{2x}{3} \right) = \frac{15x - 3}{21}</math></del> $3 + 14x = 15x - 3$ $\begin{array}{r} 3 + 14x = 15x - 3 \\ -15x \quad -15x \\ \hline -9x = -6 \\ \frac{-9x}{-9} = \frac{-6}{-9} \\ x = \frac{2}{3} \end{array}$ <p><math>-x = -6</math></p> <p><math>x = 6</math></p>	<p><u>L</u></p> $\frac{5}{6} \left( \frac{3}{8} - x \right) = 16$ $\frac{5}{16} - \frac{5}{6}x = 16$ $\begin{array}{r} \frac{5}{16} - \frac{5}{6}x = 16 \\ - \frac{5}{16} \quad - \frac{5}{16} \\ \hline -\frac{5}{6}x = \frac{251}{16} \\ x = \frac{-753}{40} \text{ OR } \\ x = -18 \frac{33}{40} \text{ OR } \end{array}$
<p><math>-x = -6</math></p> <p><math>x = 6</math></p>	<p><math>-\frac{5}{6}x = \frac{251}{16}</math></p> <p><math>x = -18.825</math></p>

B

$$x=3$$

C

$$x = -\frac{8}{7}$$

D

$$x=1$$

E

$$x=16$$

H

$$x = \frac{5}{3}$$

J

$$x = -\frac{1547}{250}, \text{ or}$$
$$x = -6\frac{47}{250}, \text{ or}$$
$$x = -6.188$$

K

$$b = \frac{3}{2} \text{ or}$$

$$b = 1.5$$

R

$$x = -8$$

S

$$x=1$$

I

$$x=1$$